## CURRICULUM RESOURCE

Masonry Math 1: Measurements and Calculations

## OALCF ALIGNMENT

| Competency | Task Group | Level |
| :--- | :--- | :--- |
| Competency A - Find and Use <br> Information | A1. Read continuous text | 2 |
| Competency A -Find and Use <br> Information | A2. Interpret documents | 2 |
| Competency B - Communicate <br> Ideas and Information | B3. Complete and create <br> documents | 2 |
| Competency C - Understand <br> and Use Numbers | C3. Use measures | 2 |

## Goal Paths (check all that apply)

$\square$ EmploymentPostsecondary
$\boxtimes$ ApprenticeshipIndependenceSecondary School Credit

## Embedded Skills for Success (check all that apply)

## Adaptability

CollaborationCommunicationCreativity and innovationDigital$\boxtimes$ Numeracy
$\boxtimes$ Problem Solving
$\boxtimes$ Reading
$\boxtimes$ Writing

NOTES: This resource is one in a series of four focused on the masonry trade. It introduces the International System of Units (SI) and how to convert one unit of measurement to another. It also outlines the dimensions of height, width, and length; the calculations for finding perimeter and area; and how to determine a 90-degree angle (based on the Pythagorean theorem). Learners should be familiar with decimal place values before using this resource.

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## Community Literacy of Ontario

## Research \& Writing

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## Units of Measurement

"The International System of Units, or SI, is the simplified and internationally accepted version of the metric system. SI holds many advantages over other systems of measurement. Decimals replace fractions, simple prefixes replace lengthy, hard to read strings of zeros, and the need for conversion
 factors (that is, numbers used to multiply or divide other numbers when converting from one measuring system to another) is entirely eliminated.

The "Textbook of Canadian Masonry" (second edition) by the Canadian Masonry Contractor's Association.

Canada adopted the International System of Units (SI) in 1971. It is used in Canadian manufacturing, architecture, engineering, and masonry construction.

SI has two parts: units and prefixes. (Remember that a prefix is always at the beginning of a word.)

SI units are measurements of length, area, volume, mass, or temperature. In masonry, they commonly include:

- Metre
- Gram
- Pascal
- Degrees Celsius

SI prefixes are symbols that represent multiples of ten. In masonry, they commonly include:

- Kilo (one thousand units)
- Centi (a one hundredth of a unit)
- Milli (a one thousandth of a unit)

When you put SI units and prefixes together, you can accurately describe a measurement without having to use a lot of zeros for large measurements or decimal points for small measurements. We will take a look at some examples on the next page.

Scenario 1: A mason is measuring the distance between their home and a job site.


The International System of Units (SI) unit they will use is metres. The SI prefix they will use is kilo, which is one thousand units. That means they know the distance they are measuring is much longer than a metre. Instead of measuring in metres, they will measure how many 1,000-metre units their home is from the job site.

If their home is 45,000 metres from the job site, it is 45 kilometres away. These numbers are the same, but the word "kilo" replaces the three zeros.

Scenario 2: A mason is measuring the length of a concrete block so they can figure out how many they need for a job.

The SI unit they will use is metres. The SI prefix they will use is centi, which is a one hundredth of a unit. That means they recognize the length they are measuring is smaller than a metre. Instead of measuring in full metres, they will measure how many one-hundredths of a metre the length of the concrete block is.


If the concrete block is 0.39 metres long, it is 39 centimetres long. These numbers are the same, but the word "centi" lets the mason record a whole number instead of using a decimal. The mason could also use "milli," which represents a one thousandth of a unit. The same concrete block is 390 millimetres long.

Scenario 3: A mason is measuring the weight (mass) of the bags sand they will use when mixing mortar.


The SI unit they will use is grams. The SI prefix they will use is kilo, which is one thousand units. That means they know each bag of sand weighs much more than a gram. Instead of measuring in grams, they will measure how many 1,000-gram units each bag of sand weighs.
If each bag of sand weighs 20,000 grams, they weigh 20 kilograms. These numbers are the same, but just like in our first example, the word "kilo" replaces the three zeros.
Note: Although we often use the words "weight" and "mass" to mean the same thing, mass is the correct word for describing how heavy an object is.

There are more International System of Units (SI) prefixes than just milli, centi, and kilo. Take a moment to read the chart below to learn about SI prefixes and what they represent.

| Prefix Name | Prefix Symbol | Number Equivalent |
| :--- | :--- | :--- |
| Mega | M | One million units |
| Kilo | k | One thousand units |
| Hecto | h | One hundred units |
| Deca | da | Ten units |
| Everything above this line represents a measurement of more than a single unit. |  |  |
| Deci | cerything below this line represents a smaller part of a unit. |  |
| Centi | m | A tenth of a unit |
| Milli | $\mu$ | A hundredth of a unit |
| Micro |  | A thousandth of a unit |

SI Prefix symbols are helpful because with them you can identify what prefix you are using without writing out the whole word. SI Units also have symbols. They are generally the first letter of the unit of measurement. Using this system, grams would be " $g$ ", and metres would be " $m$ ". This means:

- A tenth of a metre can be written as dm instead of decimetre.
- One hundred grams can be written as hg instead of hectogram.

Activity: Use the information above to answer the following questions.
How would you write the symbol for milligram? $\qquad$
What is the prefix name and symbol for 10 units? Name: $\qquad$ Symbol: $\qquad$
Two of these prefixes use the letter " m " as a symbol. The prefix with the upper-case symbol is: $\qquad$ The prefix with the lower-case symbol is: $\qquad$
What is the smallest prefix on the chart called? $\qquad$
What does it represent? $\qquad$

## Converting Measurements

Because masons use the International System of Units (SI), converting units of measurement from one prefix to another is easy. Simply move the decimal place!

This chart will show you how to do it.

| Prefix Name | Mega | Kilo | Hecto | Deca | This space | Deci | Centi | Milli | Micro |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Prefix Symbol | M | k | h | da | $\begin{gathered} =\text { one } \\ \text { unit } \end{gathered}$ | d | c | m | $\mu$ |
| Decimal Place | Move three decimal places | Move one decimal place | Move one decimal place | Move one decimal place | Move one decimal place | Move one decimal place | Move one decimal place | Move one decimal place | Move three decima places |

The decimal place always moves in the same direction as the changing prefix. If a mason was asked to convert something measured in kilometres into hectometres, they could move the decimal place one number to the right (because hecto is one spot to the right of kilo on this chart).

Note that when converting from kilo to mega, or milli to micro, the decimal will move over three places.

Tip: if a unit of measurement doesn't have a decimal in it, picture a decimal followed by a zero right after the number:

32 cm is the same as $32.0 \mathrm{~cm} \quad 427 \mathrm{~kg}$ is the same as 427.0 kg

If the mason was asked to convert 41 kilograms into hectograms, they would add the decimal and the zero at the end of 41 . Their first number would be 41.0 kg .

## 41.0 kg <br> 

The mason would then move the decimal place one number to the right.

## 410 hg

After moving the decimal place, the mason would update the SI symbol.
"One of the most versatile features of SI is the ability to convert measurements from one prefix to another simply by moving the decimal place. Converting a measurement to a different prefix can make a number more readable and easier to work with (for example 1 km instead of 1000000 mm )."

The "Textbook of Canadian Masonry" (second edition) by the Canadian Masonry Contractor's Association.

Activity: Use what you learned to convert the following units of measurement.

Convert 7.5 hectograms (hg) to decagrams (dag): $\qquad$
Convert 74.32 decimetres (dm) to centimetres (cm): $\qquad$
Convert 65922 metres (m) to kilometres (km): $\qquad$
Convert 14 milligrams (mg) to micrograms ( $\mu$ ): $\qquad$

The most common prefixes used in everyday measurements (including in the masonry trade) are kilo, centi, and milli. But it's still good to be familiar with some of the less common prefixes used in SI measurements, as in some of the examples above.

## Dimensions

Masons work in three dimensions: width, height, and length. These dimensions are important because they help masons decide how many masonry units (e.g., bricks, concrete blocks, or stones) they need to build walls in the size the job requires.


The width is the distance from the front to the back of the brick or stone.
The height is how tall the brick or stone is.
The length is how wide the brick or stone is.

For example, a Canadian Standard Residential (CSR) brick measures 90 millimetres wide, 70 millimetres high, and 230 millimetres long. This is one of the most commonly used bricks in Canada. The chart below shows the dimensions of other commonly used bricks.
$\left.\begin{array}{|c|c|c|c|c|}\hline \text { Brick Name } & \begin{array}{c}\text { Width, Height and Length } \\ \text { (in mm) }\end{array} & \text { Brick Name }\end{array} \begin{array}{c}\text { Width, Height and Length } \\ \text { (in mm) }\end{array}\right]$

Activity: Use the information in the chart to answer the following questions.

1. Circle which brick is wider: The King The CSR
2. How many millimetres wider is it? $\qquad$
3. Circle which brick is higher: The Titan The Modular
4. How many millimetres higher is it? $\qquad$
5. Circle which brick is longer: The Norman

The Giant
6. How many millimetres longer is it? $\qquad$

Masons also need to recognize the dimensions (measurements) of the project they are meant to complete. For example, they may need to build walls for a garage that is 6.7 metres in width (how far back the garage goes), 2.4 metres high, and 3.7 metres long (across the front of the garage).

Activity: Label the picture of the garage below with which dimension is its width, height, and length.


This dimension is the:
$\qquad$
"The ability to read and interpret dimensions is important whenever any construction is to be done, including masonry work. Dimensions provide the information on the size and location of different parts of the building."

The "Textbook of Canadian Masonry" (second edition) by the Canadian Masonry Contractor's Association.


## Perimeter and Area

Once a mason knows the dimensions of their masonry unit or project, they can begin calculating:

- perimeter (the distance around the outside of a shape)
- area (the amount of space inside a shape)


## Perimeter

Masons use perimeter to learn about the "footprint" of a structure's foundation and its external walls. Let's start by calculating the perimeter of the garage on the last page.

Picture yourself looking down at the garage from above. From above, the garage is a rectangle. It has four sides. Two of the sides are the same, measuring 6.7 metres each, and the other two sides are also the same, measuring 3.7 metres each.

To find out the perimeter, add up all four sides of the garage. The equation looks like this:

3.7 metres +6.7 metres +3.7 metres +6.7 metres $=20.8$ metres
$\begin{array}{lllll}\text { Side } 1 & \text { Side } 2 & \text { Side } 3 & \text { Side } 4 & \text { Perimeter }\end{array}$

The structure a mason is going to work on may not be rectangular. It may be square (with all four sides having the same measurement), or it may have more than four sides, all with different measurements. On the next page, we will look at some examples.

This structure is narrow at one end, and wide at the other. There are still four sides, but only two are the same. The shape of this structure is called a trapezoid.

To figure out the perimeter of this structure, add up all four sides just as we did for the rectangular garage. The equation looks like this:

6 metres + 4 metres + 3.5 metres + 4 metres = 17.5 metres

| Side 1 | Side 2 | Side 3 | Side 4 | Perimeter |
| :--- | :--- | :--- | :--- | :--- |



This structure is a rectangle, but it has corners that are cut at an angle. Now there are six sides to measure. Side 2 and side 6 are the same, and sides 3 and 5 are the same.

To figure out the perimeter of this structure, add up all six sides. The equation looks like this:


Activity: Calculate the perimeter of the following structures. You can use a calculator if you wish.


Structure 1: A square building. Each of the four sides is 18 metres.

| Side 1 | Side 2 | Side 3 | Side 4 | What is the |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Perimeter? |



Structure 2: A rectangular building. Two of the sides are 6.5 metres, and the other two are 8 metres.



Structure 3: A trapezoid-shaped building. Two of the sides are 11 metres, one side is 7 metres, and the other side is 3.5 metres.



Structure 4: A six-sided building. It has two sides that each measure 28 metres, and four sides that each measure 10 metres. The shape of this structure is called an irregular hexagon.
$\overline{\text { Side 1 }}+\overline{\text { Side 2 }}^{+}+\overline{\text { Side 3 }}+\overline{\text { Side 4 }}+\overline{\text { Side } 5}^{+}=\underset{\text { Side 6 }}{\substack{\text { What is the } \\ \text { Perimeter? }}}$

## Area

By looking at the height and length of the wall they need to build, a mason can also figure out its area. Masons use this information when they decide how many masonry units they will need to build the wall.

In masonry, area is measured in square units. Here are some examples:

- Square metres, which is written as $\mathrm{m}^{2}$
- Square centimetres, which is written as $\mathrm{cm}^{2}$
- Square millimetres, which is written as $\mathrm{mm}^{2}$

Let's look at an example of a calculation for finding the area of a Canadian Standard Residential (CSR) brick in square centimetres.

The CSR brick is 7 centimetres (cm) high and 23 centimetres (cm) long. Each centimetre of the height and length of the brick is shown in the image below.


To calculate the area of this brick, we will multiply the height of the brick by its width. The result will be the area of the brick in square centimetres $\left(\mathrm{cm}^{2}\right)$. Here is what that equation looks like:

| $\mathbf{2 3 ~ c m ~}$ | X | $\mathbf{7 c m}$ | $=$ | $\mathbf{1 6 1} \mathbf{~ c m}^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| Length of the brick |  | Height of the brick |  | Area of the brick |



8m
Length of the wall

To calculate the area of a wall, we will multiply how long the wall needs to be by how high the wall needs to be. For example, if a wall needs to be 8 metres (m) long and 3 metres ( m ) tall, the equation looks like this:


Calculating the area of a wall is simple when the wall is a solid square or rectangular. If a mason is working on a structure with windows and doors, they need to think about those items when figuring out the area of the wall.


To do this, the mason would first find the overall area of the wall by multiplying its height and length just as we did above. Using the wall dimensions above, the equation looks like this:

| $\mathbf{8 m}$ | $\mathbf{X}$ | $\mathbf{3 m}$ | $=$ | $\mathbf{2 4} \mathbf{m}^{\mathbf{2}}$ |
| :---: | :---: | :---: | :---: | :---: |
| Length of the wall |  | Height of the wall |  | Overall area of the wall |

Then, they would find the area of the door by multiplying its height and length. For a door that is 0.9 metres $(\mathrm{m})$ long by 2 metres $(\mathrm{m})$ high, the equation looks like this:
0.9 m
x
2 m
$=$
$1.8 \mathrm{~m}^{2}$
Length of the door
Height of the door
Area of the door

The mason would then find the area of the window by multiplying its height and length. For a window that is 0.6 metres $(\mathrm{m})$ long by 0.9 metres $(\mathrm{m})$ high, the equation looks like this:

| $\mathbf{0 . 6 ~ m}$ | $\mathbf{x}$ | $\mathbf{0 . 9 ~ m}$ | $=$ | $\mathbf{0 . 5 4 \mathrm { m } ^ { 2 }}$ |
| :---: | :---: | :---: | :---: | :---: |
| Length of the window |  | Height of the window |  | Area of the window |

Once the mason knows the area of each of these elements, they can calculate the actual area of the wall. This is done by taking away the area of the window and the door from the first calculation for the overall area of the wall. The equation looks like this:
24 m - $1.8 \mathrm{~m} \quad$ - $0.54 \mathrm{~m} \quad=\quad 21.66 \mathrm{~m}^{2}$

Overall area of the wall

Area of the door
Area of the window

Actual area of the wall

Activity: Calculate the area of the following walls. You can use a calculator if you wish.


Wall 1: A square wall that is 3 metres $(\mathrm{m})$ long and 3 metres $(\mathrm{m})$ high.

|  | $\mathbf{X}$ |  |  |
| :---: | :---: | :---: | :---: |
| What is the length <br> of the wall? |  | What is the height <br> of the wall? |  |$\quad$| What is the area |
| :---: |
| of the wall? |

Wall 2: A rectangular wall. It is 6.5 metres (m) long and 2.5 metres (m) high.

|  | $\mathbf{x}$ | $=$ |  |
| :---: | :---: | :---: | :---: |
| What is the length <br> of the wall? |  | What is the height <br> of the wall? |  |



Wall 3: A square wall that is 3.5 metres ( m ) wide and 3.5 metres ( m ) high. In that wall is a door measuring 1 metre $(\mathrm{m})$ wide and 2 metres $(\mathrm{m})$ high. There is also a window measuring 0.75 metres ( m ) wide and 1 metre ( m ) high.

First, calculate the overall area of the wall.


Then find the area of the 1 metre $(\mathrm{m})$ long and 2 metre ( m ) high door.


Now find the area of the 0.75 metre ( m ) long and 1 metre $(\mathrm{m})$ high window.


Finally, calculate the actual area of the wall.

What is the overall area of the wall?

What is the area of the door?
$\qquad$
$\qquad$ What is the area of

What is the actual area of the wall?

## Right Angles

One of a masons' daily routines is to measure right angles. A right angle is 90 degrees (also written as $90^{\circ}$ ) and it refers to the angle between two walls that come together to form a corner.
"Whether working with paint lines, chalk lines, a poured foundation or dry-laid units, it is important to check that each corner of a structure is square (that is, that it follows a $90^{\circ}$ angle) before beginning to lay the units."

The "Textbook of Canadian Masonry" (second edition) by the Canadian Masonry Contractor's Association.

A simple and reliable method for checking a 90-degree angle is called the 3-4-5 method. Here is how a mason would use this method.

First, they would measure $\mathbf{3}$ metres along one side of a corner and make a mark.

Then, they would measure 4 metres along the other side of the corner and make a mark.

Finally, the mason would measure the diagonal distance between the two marks they made. It should measure exactly 5 metres. If it doesn't, the corner is not 90 -degrees.


The 3-4-5 method can be used with any unit of measurement. The mason could measure three, four, and five millimetres, centimetres, inches, or feet. Remember, the units of measurement most often used in Canadian masonry is International System of Units (SI), so you will use metres. This simple method is based on something called the Pythagorean theorem. (The Pythagorean theorem is named after the person who discovered it hundreds of years ago. His name was Pythagorus.) As a masonry apprentice, you would use the Pythagorean theorem during in-class lessons, and on the job site.

Activity: Answer the following questions about right angles.

How is a right angle written in degrees? $\qquad$

Can the 3-4-5 method be used with any unit of measurement?

What is the name of the units of measurement most often used in Canadian masonry?

The 3-4-5 method has another name based on the person who discovered it. What is the other name?

## Conclusion

In this resource, you learned about the many ways that masons use math on the job.
Check off the information you learned about below.
$\square$ The International System of Units (SI)
$\square$ Different SI units and prefixes
$\square$ Converting from one SI prefix to another
$\square$ The dimensions of height, width, and length
$\square$ Calculating perimeter and area
$\square$ The 3-4-5 method of finding a right angle

Tip: If you didn't fill in one of the checkboxes, go back to that section and read it again. Ask a classmate, teacher, or tutor to share what they know about masonry math.

## Next Steps

For more information about becoming a brick and stone mason in Ontario, you can complete the other resources in this series:

- Professionalism in Masonry
- Tools of the Masonry Trade
- Masonry Math 2: The Next Step in Numbers

You can also visit this helpful website:

- The Canadian Masonry Contractors Association: https://canadianmasonrycontractors.com/


